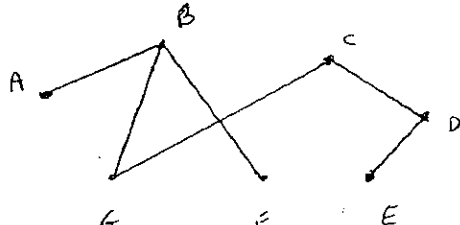
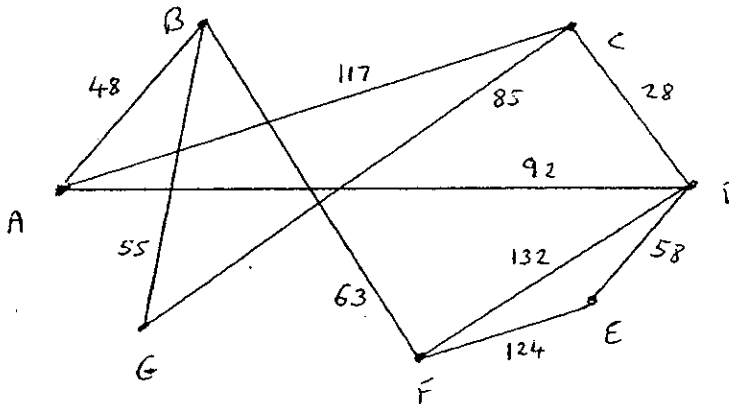


January 2006
6689 Decision D1
Mark Scheme

Question Number	Scheme	Marks
1) (a)	<p>There are 2 unmatched vertices on each side - the algorithm only matches one on each side per iteration.</p> <p>(b) e.g. $E-3=C-1$ c.s. $E=3-C=1$ $F-5=A-6=D-2=B-4$ c.s. $F=5-A=6-D=2=B-4$ $A=6$ $B=4$ $C=1$ $D=2$ $E=3$ $F=5$</p>	<p>B1 (1)</p> <p>(m) A1 (2)</p> <p>(m) A1 (2)</p> <p>(m) A1 (2)</p> <p><u>7</u></p>
2) (a)	<p>AB, BG, BF, GC, CD, DE {1 2 5 6 7 4 3}</p> <p>Weight 337m</p>  <p>(b)</p>  <p>(c)</p> <p>$AB + CF = 48 + 160 = 208$ $AC + BF = 117 + 63 = 180 *$ $AF + BC = 111 + 140 = 251$</p> <p>e.g. $\overline{ABFBGCACDEFDA}$ length $802 + 180 = 982m$</p>	<p>mi A1 A1 (3)</p> <p>B1</p> <p>B1 ✓ (2)</p> <p>mi</p> <p>A1</p> <p>A1 (3)</p> <p>mi A1</p> <p>A1</p> <p>A1 (4)</p> <p>A1</p> <p>mi A1 ✓ (3)</p> <p><u>15</u></p>

3)

A	B	n	C	D	E
1.618	-0.618	1	1.618	-0.618	1
		2	2.618	0.382	1
		3	4.236	-0.236	2
		4	6.854	0.146	3
		5	11.089	-0.090	5

Output : 1, 1, 2, 3, 5

m₁
A₁ A₁ (3)
m₁ A₁ ✓
A₁ ✓
A₁
A₁ (5)
A₁ ✓ (1)
9

4) a)

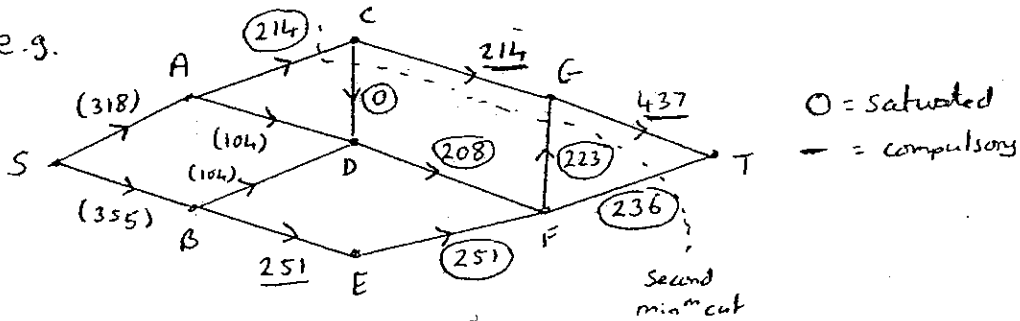
(i) A cut is a division of the vertices of a flow network into 2 sets, one containing the source (s) and the other containing the sink (t).

(ii) A cut whose capacity is least

B₁
B₁ (2)
B₁, B₂, 0
(3)

(b) $C_1 = 1038$, $C_2 = 673$

(c) e.g.



m₁
A₁
A₁ (3)

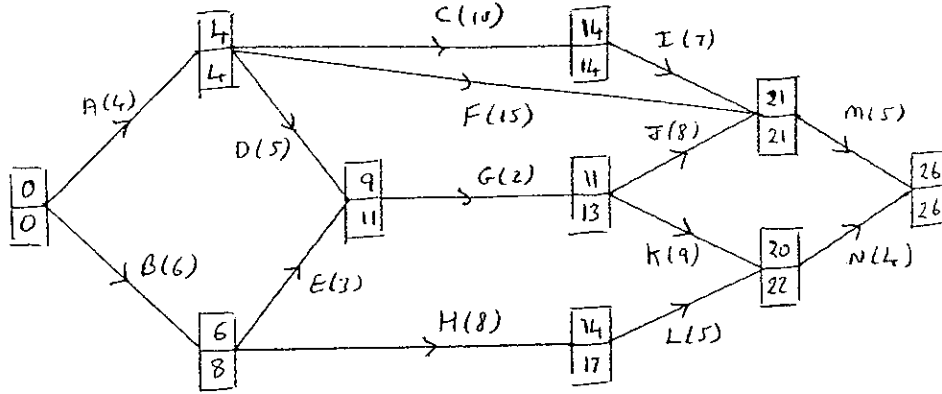
(d) AC, CD, GF, FT

(e) DE would not allow any further flow into EF

DG would cross both minimum cuts - D contains extra flow, G T can accept it. Flow increases by 86 to 759 (accept either number)

B₁ (1)
B₂, 1, 0
(2)
11

5 (a)



M1 A1

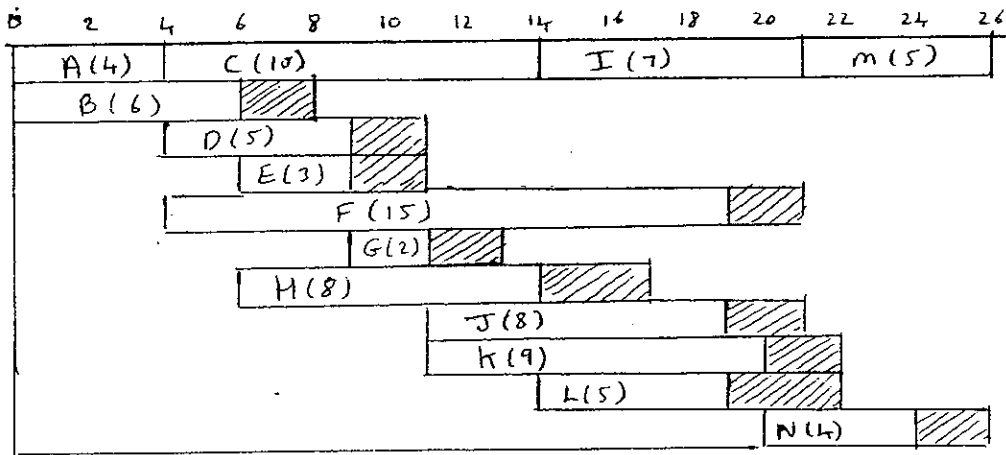
M1 A1

(4)

(b) A C I m length 26

B1 B1 ✓ (2)

(c)



M1

A3, 2/10

(4)

(d)

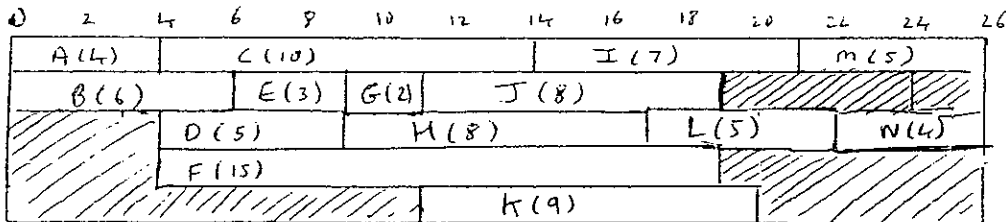
5 workers needed e.g. ref to 13-14 when C, F, H, J and K must be taking place
e.g. ref to 18-19 when I, F, J, K, L must be taking place

B2, 1, 0

(2)

(e)

e.g.



M1

A2, 1, 0

(3)

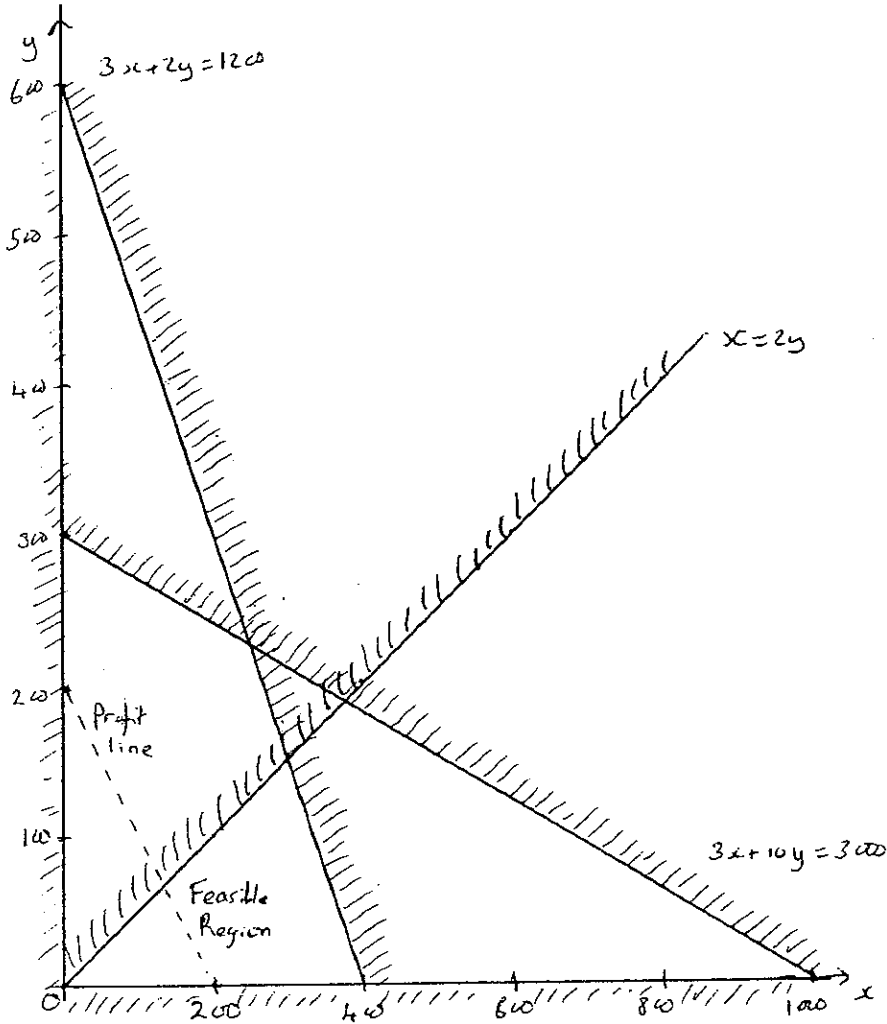


15

6. a) Maximise, $(P=) 15x + 15y$
 Subject to $3x + 10y \leq 3000$
 $3x + 2y \leq 1200$
 $x \geq 2y$
 $x, y \geq 0$

B1, B1
 B3, 2, 1, 0
 (5)

(b)



B6, 5, 4, 3, 2, 1, 0

(6)

- (c) Profit line or vertex testing, $(300, 150)$, profit = £ 67.50
 (d) Production of stickers should be increased since this would move the intersection point further from the origin.
 (e) e.g. The constraint lines would be far outside the feasible region - so they would not affect it.

M1 A1/A1 (3)

B2, 1/0 (2)

B2, 1/0 (2)

18